



New Encryption Algorithm Based on Network RFWKIDEA8-1 Using Transformation of AES Encryption Algorithm

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ABSTRACT

In this article we developed a new block encryption algorithm based on network RFWKIDEA8-1 using of the transformations of the encryption algorithm AES, which is called AES- RFWKIDEA8-1. The block's length of this encryption algorithm is 256 bits; the numbers of rounds are 10, 12 and 14. The advantages of the encryption algorithm AES- RFWKIDEA8-1 are that, when encryption and decryption process used the same algorithm. In addition, the AES-RFWKIDEA8-1 encryption algorithm encrypts faster than AES.

Keywords: *Advanced Encryption Standard, Feystel Network, Lai–Massey Scheme, Round Function, Round keys, Output Transformation, Multiplicative Inverse, Additive Inverse.*

1 INTRODUCTION

In September 1997 the National Institute of Standards and Technology (NIST) issued a public call for proposals for a new block cipher to succeed the Data Encryption Standard (DES) [4]. Out of 15 submitted algorithms the Rijndael cipher by Daemen and Rijmen [1] was chosen to become the new Advanced Encryption Standard (AES) in November 2001 [2]. The Advanced Encryption Standard is a block cipher with a fixed block length of 128 bits. It supports three different key lengths: 128 bits, 192 bits, and 256 bits. Encrypting a 128-bit block means transforming it in n rounds into a 128-bit output block. The number of rounds n depends on the key length: $n = 10$ for 128-bit keys, $n = 12$ for 192-bit keys, and $n = 14$ for 256-bit keys. The 16-byte input block (t_0, t_1, \dots, t_{15}) which is transformed during encryption is usually written as a 4x4 byte matrix, the called AES State.

t_0	t_4	t_8	t_{12}
t_1	t_5	t_9	t_{13}
t_2	t_6	t_{10}	t_{14}
t_3	t_7	t_{11}	t_{15}

The structure of each round of AES can be reduced to four basic transformations occurring to

the elements of the State. Each round consists in applying successively to the State the SubBytes(), ShiftRows(), MixColumns() and AddRoundKey() transformations. The first round does the same with an extra AddRoundKey() at the beginning whereas the last round excludes the MixColumns() transformation.

The SubBytes() transformation is a nonlinear byte substitution that operates independently on each byte of the *State* using a substitution table (S-box). Figure 1 illustrates the SubBytes() transformation on the *State*.

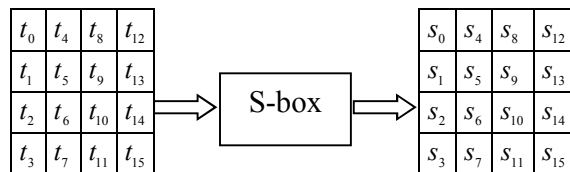


Fig. 1. SubBytes() transformation

In the ShiftRows() transformation operates on the rows of the *State*; it cyclically shifts the bytes in each row by a certain offset. For AES, the first row is left unchanged. Each byte of the second row is shifted one to the left. Similarly, the third and fourth rows are shifted by offsets of two and three respectively. Figure 2 illustrates the ShiftRows() transformation.

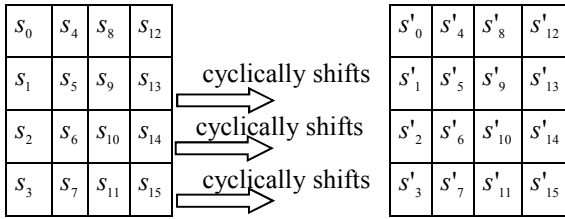


Fig. 2. ShiftRows() transformation.

The MixColumns() transformation operates on the *State* column-by-column, treating each column as a four-term polynomial. The columns are considered as polynomials over $GF(2^8)$ and multiplied modulo $x^4 + 1$ with a fixed polynomial $a(x)$, given by $a(x) = 3x^2 + x^2 + x + 2$. Let $p = a(x) \otimes s'$:

$$\begin{bmatrix} p_{4i} \\ p_{4i+1} \\ p_{4i+2} \\ p_{4i+3} \end{bmatrix} = \begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s'_{4i} \\ s'_{4i+1} \\ s'_{4i+2} \\ s'_{4i+3} \end{bmatrix}, i = \overline{0 \dots 3}$$

As a result of this multiplication, the four bytes in a column are replaced by the following:

$$\begin{aligned} y_{4i} &= (\{02\} \bullet s'_{4i}) \oplus (\{03\} \bullet s'_{4i+1}) \oplus s'_{4i+2} \oplus s'_{4i+3} \\ y_{4i+1} &= s'_{4i} \oplus (\{02\} \bullet s'_{4i+1}) \oplus (\{03\} \bullet s'_{4i+2}) \oplus s'_{4i+3} \\ y_{4i+2} &= s'_{4i} \oplus s'_{4i+1} \oplus (\{02\} \bullet s'_{4i+2}) \oplus (\{03\} \bullet s'_{4i+3}) \\ y_{4i+3} &= (\{03\} \bullet s'_{4i}) \oplus s'_{4i+1} \oplus s'_{4i+2} \oplus (\{02\} \bullet s'_{4i+3}). \end{aligned}$$

Figure 3 illustrates the MixColumns() transformation.

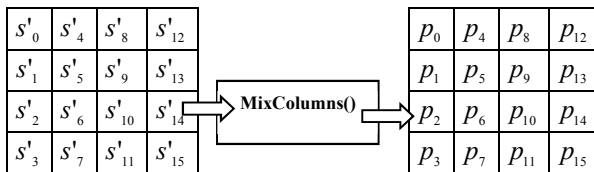


Fig. 3. MixColumns() transformation.

Description network RFWKIDEA8-1 given in [3] and, similarly as in the Feistel network, when it encryption and decryption using the same algorithm. In the network used one round function having four input and output blocks and as the round function can use any transformation.

In this paper developed block encryption algorithm AES-RFWKIDEA8-1 based network RFWKIDEA8-1 using transformation of the encryption algorithm AES. The length of block of

the encryption algorithm AES-RFWKIDEA8-1 is 256 bits, the number of rounds n equal to 10, 12, 14 and the length of key is variable from 256 bits to 1024 bits in steps 128 bits, i.e. key length is equal to 256, 384, 512, 640, 768, 896 and 1024 bits.

2 THE STRUCTURE OF THE ENCRYPTION ALGORITHM AES-RFWKIDEA8-1

In the encryption algorithm AES-RFWKIDEA8-1 as the round function used SubBytes(), ShiftRows(), MixColumns() transformation of the encryption algorithm AES. The scheme n -rounded encryption algorithm AES-RFWKIDEA8-1 shown in Figure 4, and the length of subblocks X^0, X^1, \dots, X^7 , length of round keys $K_{8(i-1)}, K_{8(i-1)+1}, \dots, K_{8(i-1)+7}, i = \overline{1 \dots n+1}$ and $K_{8n+8}, K_{8n+9}, \dots, K_{8n+23}$ are equal to 32 bits.

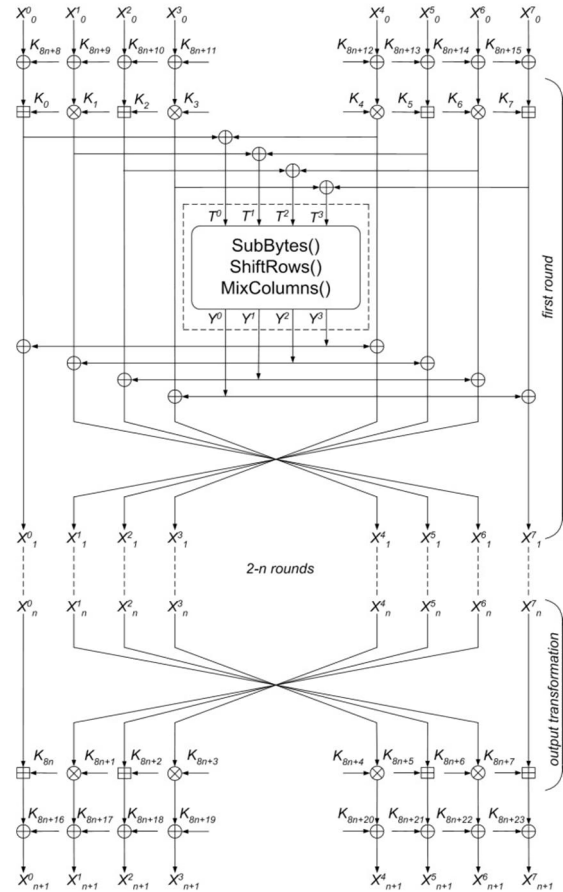


Fig. 4. The scheme n -rounded encryption algorithm AES-RFWKIDEA8-1

Consider the round function of the encryption algorithm AES-RFWKIDEA8-1. Initially 32-bit

subblocks T^0, T^1, T^2, T^3 , are partitioned into 8-bit subblocks, i.e., on bytes:

$$\begin{aligned}
 t_0 &= sb_0(T^0), & t_1 &= sb_1(T^0), & t_2 &= sb_2(T^0), \\
 t_3 &= sb_3(T^0), & t_4 &= sb_0(T^1), & t_5 &= sb_1(T^1), \\
 t_6 &= sb_2(T^1), & t_7 &= sb_3(T^1), & t_8 &= sb_0(T^2), \\
 t_9 &= sb_1(T^2), & t_{10} &= sb_2(T^2), & t_{11} &= sb_3(T^2), \\
 t_{12} &= sb_0(T^3), & t_{13} &= sb_1(T^3), & t_{14} &= sb_2(T^3), \\
 t_{15} &= sb_3(T^3), & \text{here } sb_0(X) &= x_0x_1\dots x_7, \\
 sb_1(X) &= x_8x_9\dots x_{15}, & sb_2(X) &= x_{16}x_{17}\dots x_{23}, \\
 sb_3(X) &= x_{24}x_{25}\dots x_{31} \text{ and } X = x_0x_1\dots x_{31}.
 \end{aligned}$$

After which the 8-bit subblocks t_0, t_1, \dots, t_{15} are written into the array *State* and are executed the above transformations SubBytes(), ShiftRows(), MixColumns().

After the MixColumns() transformation we obtain 8-bits subblocks p_0, p_1, \dots, p_{15} . The resulting 8-bit subblocks are written on a 32-bit subblocks Y^0, Y^1, Y^2, Y^3 as follows:

$$\begin{aligned}
 Y^0 &= p_0 \parallel p_1 \parallel p_2 \parallel p_3, & Y^1 &= p_4 \parallel p_5 \parallel p_6 \parallel p_7 \\
 Y^2 &= p_8 \parallel p_9 \parallel p_{10} \parallel p_{11}, & Y^3 &= p_{12} \parallel p_{13} \parallel p_{14} \parallel p_{15}.
 \end{aligned}$$

The S-box SubBytes() transformation shown in Table 1 and is the only nonlinear transformation. The length of the input and output blocks S-box is eight bits. For example, if the input value the S-box is equal to 0xE7, then the output value is equal 0xFA, i.e. selected elements of intersection row 0xE and column 0x7.

Table 1: The S-box of encryption algorithm AES-RFWKIDEA8-1

0x0	0x1	0x2	0x3	0x4	0x5	0x6	0x7	0x8	0x9	0xA	0xB	0xC	0xD	0xE	0xF
0x0	0x7F	0x0F	0x6B	0x38	0x36	0x05	0xF1	0x5B	0x37	0x47	0x8B	0x4A	0xB8	0x8F	0xED
0x1	0xEF	0xDA	0x05	0x25	0x4C	0x4F	0x15	0xDF	0xF0	0xB5	0x44	0x19	0x80	0x59	0x91
0x2	0x5E	0x82	0x34	0x17	0x2A	0x83	0x11	0xF2	0xC3	0x8A	0xC5	0x0C	0xAB	0x3B	0xE4
0x3	0x60	0xB2	0x30	0x46	0xD3	0x13	0xB3	0x9D	0x5A	0x40	0x33	0x0B	0xA2	0xC4	0x79
0x4	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x	0x0x
0x4	0x3D	0x09	0x84	0x3A	0xE9	0x22	0x75	0xAD	0x0F	0x77	0x5C	0xAA	0xA3	0xD8	0xBE
0x5	0xDC	0x92	0x94	0xBF	0x0A	0x51	0x43	0xA6	0xD6	0x3C	0xF7	0x9E	0x48	0x55	0x9C
0x6	0x41	0x56	0x3E	0x9F	0xE1	0x86	0x0D	0x14	0xFC	0x76	0x7D	0xCC	0xE6	0xB9	0xBA
0x7	0x35	0x97	0xDB	0x87	0xE7	0x53	0x4D	0xF8	0x1E	0x8D	0xD2	0xD9	0xA9	0x6B	0xE5
0x8	0x21	0x1A	0x93	0x6C	0x52	0xC0	0x2F	0x67	0x88	0x63	0x1F	0x6A	0xB1	0xBB	0x00
0x9	0x45	0xE0	0x6F	0xCF	0xE3	0x99	0x0E	0x49	0xC6	0x85	0xEA	0x5D	0x26	0x81	0xD4

0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0	0x0
A	E2	DE	A4	07	72	89	FE	68	95	7B	23	AC	DD	29	16
B	2C	06	F9	18	6E	66	BC	04	CB	FB	2B	71	62	EB	CA
C	03	02	2D	6D	27	B0	64	61	98	1C	8C	1D	9B	CD	73
D	78	50	B7	58	A1	AE	C2	F3	96	10	28	39	2E	AF	F4
E	31	A5	74	7A	EC	E8	54	FA	4E	CE	FD	4B	1B	C1	70
F	BD	7E	9A	C9	24	FF	32	3F	08	A7	57	20	90	12	D0

Consider the encryption process of encryption algorithm AES-RFWKIDEA8-1. Initially the 256-bit plaintext X partitioned into subblocks of 32-bits $X_0^0, X_0^1, \dots, X_0^7$, and performs the following steps:

1) subblocks $X_0^0, X_0^1, \dots, X_0^7$ summed by XOR respectively with round key $K_{8n+8}, K_{8n+9}, \dots, K_{8n+15}$: $X_0^j = X_0^j \oplus K_{8n+8+j}, i = \overline{0\dots7}$

2) subblocks $X_0^0, X_0^1, \dots, X_0^7$ multiplied and summed respectively with the round key $K_{8(i-1)}, K_{8(i-1)+1}, \dots, K_{8(i-1)+7}$ and calculated 32-bit subblocks T^0, T^1, T^2, T^3 . This step can be represented as follows:

$$\begin{aligned}
 T^0 &= (X_{i-1}^0 + K_{8(i-1)}) \oplus (X_{i-1}^4 \cdot K_{8(i-1)+4}), \\
 T^1 &= (X_{i-1}^1 \cdot K_{8(i-1)+1}) \oplus (X_{i-1}^5 + K_{8(i-1)+5}), \\
 T^2 &= (X_{i-1}^2 + K_{8(i-1)+2}) \oplus (X_{i-1}^6 \cdot K_{8(i-1)+6}), \\
 T^3 &= (X_{i-1}^3 \cdot K_{8(i-1)+3}) \oplus (X_{i-1}^7 + K_{8(i-1)+7}), i = \overline{1}.
 \end{aligned}$$

3) subblocks T^0, T^1, T^2, T^3 is split into 8-bit subblocks t_0, t_1, \dots, t_{15} and performed SubBytes(), ShiftRows(), MixColumns(), AddRoundKey() transformations. Output subblocks of the round function of the encryption algorithm are Y^0, Y^1, Y^2, Y^3 .

4) subblocks Y^0, Y^1, Y^2, Y^3 are summed to XOR with subblocks $X_{i-1}^0, X_{i-1}^1, \dots, X_{i-1}^7$, i.e. $X_{i-1}^j = X_{i-1}^j \oplus Y_{3-j}^j, X_{i-1}^{j+4} = X_{i-1}^{j+4} \oplus Y_{3-j}^j, j = \overline{0\dots3}$,

5) at the end of the round subblocks X_{i-1}^1 and X_{i-1}^6, X_{i-1}^2 and X_{i-1}^5, X_{i-1}^3 and X_{i-1}^4 swapped, X_{i-1}^0 and X_{i-1}^7 does not change,

6) repeating steps 2-5 n times, i.e., $i = \overline{2...n}$ we obtain subblocks $X_n^0, X_n^1, \dots, X_n^7$.

7) in output transformation round keys are multiplied and summed into subblocks, i.e.
 $X_{n+1}^0 = X_n^0 + K_{8n}$, $X_{n+1}^1 = X_n^6 \cdot K_{8n+1}$,
 $X_{n+1}^2 = X_n^5 + K_{8n+2}$, $X_{n+1}^3 = X_n^4 \cdot K_{8n+3}$,
 $X_{n+1}^4 = X_n^3 \cdot K_{8n+4}$, $X_{n+1}^5 = X_n^2 + K_{8n+5}$,
 $X_{n+1}^6 = X_n^1 \cdot K_{8n+6}$, $X_{n+1}^7 = X_n^7 + K_{8n+7}$.

8) subblocks $X_{n+1}^0, X_{n+1}^1, \dots, X_{n+1}^7$ are summed to XOR with the round key $K_{8n+16}, K_{8n+17}, \dots, K_{8n+23}$: $X_{n+1}^j = X_{n+1}^j \oplus K_{9n+16+j}$, $j = \overline{0...7}$. As cipher text plaintext X receives the combined 32-bit subblocks $X_{n+1}^0 \parallel X_{n+1}^1 \parallel \dots \parallel X_{n+1}^7$

3 KEY GENERATION OF THE ENCRYPTION ALGORITHM AES-RFWKIDEA8-1

In the n -round encryption algorithm AES-RFWKIDEA8-1 in each round applied of eight round keys to 32 bits and output conversion eight round keys of 32 bits. In addition, before to the first round and after the output transformations is used eight round keys of 32 bits. Total number of 32-bit round key is equal to $8n + 24$. When encoding in Figure 4 is used instead of K_i encryption round keys K_i^c , while decryption round decryption key K_i^d .

When generating round keys like the AES encryption algorithm uses an array Rcon:

Rcon=[0x00000001, 0x00000002, 0x00000004, 0x00000008, 0x00000010, 0x00000020, 0x00000040, 0x00000080, 0x00000100, 0x00000200, 0x00000400, 0x00000800, 0x00001000, 0x00002000, 0x00004000, 0x00008000, 0x00010000, 0x00020000, 0x00040000, 0x00080000, 0x00100000, 0x00200000, 0x00400000, 0x00800000, 0x01000000, 0x02000000, 0x04000000, 0x08000000, 0x10000000, 0x20000000, 0x40000000, 0x80000000].

The key encryption algorithm K of length l ($256 \leq l \leq 1024$) bits is divided into 32-bit round keys $K_0^c, K_1^c, \dots, K_{Lenght-1}^c$, $Lenght = l/32$, here

$K = \{k_0, k_1, \dots, k_{l-1}\}$, $K_0^c = \{k_0, k_1, \dots, k_{31}\}$,
 $K_1^c = \{k_{32}, k_{33}, \dots, k_{63}\}$, \dots , $K_{Lenght-1}^c = \{k_{l-32}, k_{l-31}, \dots, k_{l-1}\}$
and $K = K_0^c \parallel K_1^c \parallel \dots \parallel K_{Lenght-1}^c$. After which

calculated $K_L = K_0^c \oplus K_1^c \oplus \dots \oplus K_{Lenght-1}^c$. If $K_L = 0$ then K_L is chosen as 0x5C5C31537, i.e. $K_L = 0x5C5C31537$. When generating a round key K_i^c , $i = \overline{Lenght...8n+23}$, we used transformation $SubBytes32()$ and $RotWord32()$, here $SubBytes32()$ -is transformation 32-bit subblock into S-box and $SubBytes32(X) = S(sb_0(X)) \parallel S(sb_1(X)) \parallel S(sb_2(X)) \parallel S(sb_3(X))$, $RotWord32()$ -cyclic shift to the left of 1 bit of the 32 bit subblock. When the condition $i \bmod 3 = 1$ is true, then the round keys are computed as
 $K_i^c = SubBytes32(K_{i-Lenght+1}^c) \wedge SubBytes32(RotWord32(K_{i-Lenght}^c)) \wedge Rcon[i \bmod 32] \wedge K_L$,
otherwise $K_i^c = SubBytes32(K_{i-Lenght}^c) \wedge SubBytes32(K_{i-Lenght+1}^c) \wedge K_L$. After each round key generation the value K_L is cyclic shift to the left by 1 bit.

Decryption round keys are computed on the basis of encryption round keys and decryption round key the first round associated with of encryption round keys as follows:

$(K_0^d, K_1^d, K_2^d, K_3^d, K_4^d, K_5^d, K_6^d, K_7^d) = (-K_{8n}^c, (K_{8n+1}^c)^{-1}, -K_{8n+2}^c, (K_{8n+3}^c)^{-1}, (K_{8n+4}^c)^{-1}, -K_{8n+5}^c, (K_{8n+6}^c)^{-1}, -K_{8n+7}^c)$.

A decryption keys the output transformation associated with of encryption round keys as follows:

$(K_{8n}^d, K_{8n+1}^d, K_{8n+2}^d, K_{8n+3}^d, K_{8n+4}^d, K_{8n+5}^d, K_{8n+6}^d, K_{8n+7}^d) = (-K_0^c, (K_1^c)^{-1}, -K_2^c, (K_3^c)^{-1}, (K_4^c)^{-1}, -K_5^c, (K_6^c)^{-1}, -K_7^c)$.

Likewise, the decryption key of the second, third, and n -round associated encryption round keys with the following:

$(K_{8(i-1)}^d, K_{8(i-1)+1}^d, K_{8(i-1)+2}^d, K_{8(i-1)+3}^d, K_{8(i-1)+4}^d, K_{8(i-1)+5}^d, K_{8(i-1)+6}^d, K_{8(i-1)+7}^d) = (-K_{8(n-i+1)}^c, (K_{8(n-i+1)+6}^c)^{-1}, -K_{8(n-i+1)+5}^c, (K_{8(n-i+1)+4}^c)^{-1}, (K_{8(n-i+1)+3}^c)^{-1}, -K_{8(n-i+1)+2}^c, (K_{8(n-i+1)+1}^c)^{-1}, -K_{8(n-i+1)+7}^c)$, $i = \overline{2...n}$.

Decryption round keys applied to the first round and after the output transformation associated with the encryption round keys as follows:

$K_{8n+8+j}^d = K_{8n+16+j}^c$, $K_{8n+16+j}^d = K_{8n+8+j}^c$, $j = \overline{0...7}$.

4 RESULTS

Using the transformations $SubBytes()$, $ShiftRows()$, $MixColumns()$ of the encryption algorithm AES as the round transformation network

RFWKIDEA8-1 we developed block cipher algorithm AES-RFWKPES8-1. In the algorithm, the number of rounds of encryption and key's length is variable and the user can select the number of rounds and the key's length in dependence of the degree of secrecy of information and speed encryption.

As in the encryption algorithms based on the Feistel network, the advantages of the encryption algorithm RFWKIDEA8-1 are that, when encryption and decryption process used the same algorithm. In the encryption algorithm RFWKIDEA8-1 in decryption process encryption round keys are used in reverse order, thus on the basis of operations necessary to compute the inverse. For example, if the round key is multiplied by the subblock, while decryption is necessary to calculate the multiplicative inverse, if summarized, it is necessary to calculate the additive inverse.

It is known that the resistance of AES encryption algorithm is closely associated with resistance S-box, applied in the algorithm. In the S-box's encryption algorithm AES algebraic degree of nonlinearity $\text{deg} = 7$, nonlinearity $NL = 112$, resistance to linear cryptanalysis $\lambda = 32/256$, resistance to differential cryptanalysis $\delta = 4/256$, strict avalanche criterion $SAC = 8$, bit independence criterion $BIC = 8$.

In the encryption algorithm AES-RFWKIDEA8-1 resistance S-box is equal to resistance S-box's encryption algorithm AES, i.e., $\text{deg} = 7$, $NL = 112$, $\lambda = 32/256$, $\delta = 4/256$, $SAC = 8$, $BIC = 8$.

Research indicates that the speed of the encryption algorithm AES-RFWKIDEA8-1 is faster than AES. The encryption speed of the 14 rounds encryption algorithm AES-RFWKIDEA8-1 1.25 times faster than the 14 rounds encryption algorithm AES.

5 CONCLUSIONS

It is known that as a network-based algorithms Feistel the resistance algorithm based on network RFWKIDEA8-1 closely associated with resistance round function. Therefore, selecting the transformations `SubBytes()`, `ShiftRows()`, `MixColumns()` of the encryption algorithm AES, based on round function network RFWKIDEA8-1 we developed relatively resistant encryption algorithm.

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