An Efficient ECC-based Authentication and Key Agreement Protocol

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ABSTRACT

Public-key cryptography is commonly used to authenticate communicating entities in some networks. One of the key tools in this way is to use the elliptic curves cryptography (ECC) which is relatively lightweight due to its shorter key size compared to the conventional River-Shamir-Adleman (RSA) method. This paper is proposing an efficient protocol by analyzing two variants of ECC-based wireless authentication protocol, namely, Aydos-Savas-Koc's wireless authentication protocol (ASK-WAP) and user authentication protocol (UAP) from various security aspects and communication concerns. We show that although UAP is able to address some of ASK-WAP vulnerabilities, it is confined to one-way communication where the authentication can only be initialized by users and not the server. In light of their limitations, we suggest several possible improvements to both ASK-WAP and UAP. The proposed solutions focus on applying encryption methods to the transmitted keys and enabling two-way communication on UAP. From performance evaluation, we show that our proposed methods are able to address the security concerns of ASK-WAP and UAP, while at the same time achieving acceptable communication overheads.

Keywords: Elliptic Curves Cryptography, ASK-WAP, UAP.

1 INTRODUCTION

Providing adequate security is a challenging issue for many types of communication networks. Among them, those that are using air interface or internet (such as wireless communications, wireless sensor networks, voice over IP, etc.) are more prone to various types of security attacks. In general, wireless networks do not provide the same level of protection as wired networks. Due to using air interface, they are vulnerable to several attacks, including: unauthorized use of resources, masquerading, unauthorized disclosure and flow data information, unauthorized alteration of resources and data information, repudiation of actions, and denial of service attacks.

To enhance the security of wireless networks, public-key cryptography can be used for authentication. In this regard, securing communications between users and certification authority (CA) is one of the concerns in wireless networks. Compared to private-key/symmetric-key systems, public-key systems (i.e., based on certificates) ensure stronger security, but suffer from more computational cost and power [1]. To balance the security and efficiency, an efficient authentication is therefore required for inclusion in wireless networks.

One promising approach is to use elliptic curve cryptography (ECC) which provides striking advantage of shorter key size compared to conventional algorithm (e.g., RSA algorithm), while preserving the equivalent security level. Additionally, ECC has been accepted as IEEE P1363 Standard for Public Key Cryptography [2]. Recently, some authentication and key agreement protocol based on ECC have been proposed [3-6]. On the other hand, several EC-based cryptography methods are proposed for wireless sensor networks [7] as well as session initiation protocol [8].
In [9] Aydos et al. an ECC-based wireless authentication and key agreement protocol called ASK-WAP have been proposed for securing user-server communication. While their proposed ASK-WAP has several advantages in terms of storage requirements, bandwidth, and computational burden, it is also vulnerable to several attacks such as man-in-the-middle attack [10], lack of mutual authentication [2] and forward secrecy [11], and prone to forging certificate attack [12]. This led to a new wireless authentication protocol called user authentication protocol (UAP) [10][13].

In this paper, we analyze both ASK-WAP and UAP schemes and show that although UAP is able to overcome some of the security concerns faced by ASK-WAP, has another problem and isn’t the best solution for ASK-WAP. One of the biggest problems of UAP is its one-way nature where the communication can only be initialized by users (i.e., server has no control over the communication). Therefore, it is also prone to denial of service attack, known-text and chosen-text attacks, as well as exhaustive attack. We improve both ASK-WAP and UAP by proposing some derivations to solve the security and communication problems.

The rest of the paper is structured as follows. Some common definitions and abbreviations are summarized as bellow. In Section 2, two existing protocols, namely, ASK-WAP and UAP are discussed in details followed by highlighting their efficiencies and weaknesses. Our proposed algorithms are explained in Section 3. The performance evaluation is discussed in Section 4, followed by some concluding remarks.

**Definitions:**

- **U**: User
- **S**: Server
- **d**: Private Key (an integer).
- **H(k,m)**: One-way Hash function.
- **E(k,m)**: Encrypt plaintext m by key k.
- **D(k,m)**: Decrypt cipher text m by key k.
- **t**: time stamp
- **I**: identifier
- **M**: A point (M.x, M.y) on the Elliptic Curve that is chosen as Public Key.
- **B**: base point on the Elliptic Curves by order n that is known for all parties.
- **d*B**: multiply integer d by point B using ECC’s specific rules.
- **g**: Random number.
- **(r,s)**: special certificates for use in Elliptic Curve Digital Signature Algorithm (ECDSA).

## 2 EXISTING PROTOCOLS

### 2.1 ASK-WAP

ASK-WAP uses the Elliptic Curve Diffie-Hellman (ECDH) for key substitute/exchange and Elliptic Curve Digital signature Algorithm (ECDSA) for signing and verification. In the initialization section the users and the server obtain their certificates (r,s) for use in ECDSA, identifiers (I), and expiration dates from the Certification Authority (CA) throughout a secure channel. This is done just one time during the expiration time.

To apply Elliptic Curves, a curve over a Galois field $GF(p)$ where p is a prime number or over $GF(2^n)$ where q is an integer should be defined. The first one is suitable to be implemented in software while the second one is compatible with hardware [11]. To prevent known attacks, one must pay enough attention in choosing curve’s coefficients. The National Institute of Standards and Technology (NIST) has recommended some prime numbers in Federal Information Processing Standard 186-2 (FIPS 186-2) standard [14]. In an Elliptic Curve group a base point $B (B_x, B_y)$ of large order n should be selected and made public to all parties. In the initialization parts, user can select a random number $d_U$ as its private key and calculate its public key $M_U = d_U \times B$ by performing point doubling and multiplying rules. Also server can calculate $M_S = d_S \times B$ in a similar manner.

In the key agreement part, user and server can exchange their public key. User can calculate $d_U \times M_S = (d_U, d_s) \times B$, server also can calculate $d_S \times M_U = (d_s, d_j) \times B$. Now they can agree on $(d_U, d_S) \times B$ as their mutual key.

### 2.2 UAP

Because of ASK-WAP’s weaknesses such as its vulnerability against man-in-the-middle attack (to be discussed in the next subsection), Mangipudi et al. proposed a variant of it in [10]. They simply calculate another random numbers $g_U$ and $g_S$ in user and server parts. User sends $M_R = g_U \times M_S = (g_U, d_s) \times B$ to the server but agrees on $g_U \times B$. Server can calculate $d_S \times M_R = (d_s, g_U, d_s) \times B = g_U \times B$ to get the mutually agreed key.

### 2.3 Analysis of ASK-WAP and UAP

Several security requirements for an authentication and key agreement protocol in wireless communication are defined in [9], which
are nonrepudiation of service, mutual authentication, confidentiality, and anonymity of user.

ASK-WAP doesn’t provide mutual authentication [2] due to using Diffie-Hellman (DH) key exchange protocol in its initialization phase, which is vulnerable against man-in-the-middle and impersonating attacks. Since ASK-WAP and UAP both offers digital signature, the non-reputation of services can be achieved. Both protocols achieved confidentiality by protecting data transmitted between two parties. They also have the capability of using a temporary identity assigned by CA to the user, so they can meet the anonymity of user.

Both ASK-WAP and UAP do not meet known-key security, since the long-term session key ($M_{K-x}$) can be easily compromised. In addition, ASK-WAP doesn’t provide forward secrecy [11], and neither does UAP because by compromising the server’s private key all session keys can be recovered as well.

2.4 Other Weaknesses of UAP

In addition, UAP has other weaknesses as follow:

- Only user can initialize the communication. It should be noted that in certain cases server needs to do it as well, e.g., for call terminating. Although it is not a security weakness, it can be regarded as a major communication problem, and thus the protocol may not be feasible to be implemented at all.

- At the beginning of the initialization session, users do not send any information (for example its permanent public key or its certificate) to the server. Even in the next steps user’s identifier is never used, thus an adversary/attacker can easily launch a Denial-of-Service (DoS) attack. Attacker can send huge number of requests to the server and confusing it by calculating mutually agreed keys.

- The algorithm uses the mutual key as the encryption key and a part of the plain-text of the block cipher simultaneously to encrypt the text. This accelerates the known-text and chosen-text attacks against the block cipher. An adversary can easily break it knowing that the major part of the plain-text is the same as the key.

- Suppose that the long term session key, i.e., mutual key, is compromised by knowing one’s $M_K$ that is available because it is sent clear. The adversary can recover the server’s private key. Because $M_S = (g_U d_S) \times B$, and adversary knows the $g_U$, thus, adversary can even launch the exhaustive attack easily to find a multiplicative of $g_U$ that meets the above equation.

3 IMPROVEMENTS AND SUGGESTIONS

In this section, we suggest three new possible ways to improve the ASK-WAP. Then we introduce a robust way to improve UAP protocol.

3.1 First Proposal - EKE-ASK

Pre-shared password idea was used by P. Koduri [12] called EC-EKE (Elliptic Curve Encrypted Key Exchange) which considers a predetermined block cipher and a pre-shared password ‘s’ as its key, namely:

User 1 computes $M_1 = d_s \times B$ and sends $E(s, M_1)$ to user 2.
User 2 computes $M_2 = d_s \times B$ and sends $E(s, M_2)$ to user 1.

If we apply EC-EKE idea to ASK-WAP, by encrypting $M_U$ and $M_S$ before exchanging them, we will solve almost all its problems. It will foil man-in-the-middle attack (i.e., one of the main weaknesses of ASK-WAP). The two remained problems are; i) possessing and saving shared password ‘s’ in subscriber Identity Module (SIM) of both sides, and ii) encrypting a point by the block cipher algorithm. To solve this problem, we can represent the points in compressed forms as in [15]. Figure 1 illustrates its mutual authentication phase, and the main changes to ASK-WAP are shown in bold.

<table>
<thead>
<tr>
<th>User</th>
<th>Server</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Send E(s, M_U)</td>
<td>Receive E(s, M_U)</td>
</tr>
<tr>
<td></td>
<td>$M_U = D(s, M_U)$</td>
</tr>
<tr>
<td>2.</td>
<td>Generate a random number</td>
</tr>
<tr>
<td></td>
<td>$g_S \in {2, n-2}$</td>
</tr>
<tr>
<td>3. Receive E(s, M_S, g_S)</td>
<td>Send E(s, M_S, g_S)</td>
</tr>
<tr>
<td>$M_S, g_S = D(s, M_S, g_S)$</td>
<td></td>
</tr>
<tr>
<td>4. $M_K = d_U \times M_S$</td>
<td>$M_K = d_S \times M_U$</td>
</tr>
<tr>
<td>$(d_U d_S) \times B$</td>
<td>$(d_S d_U) \times B$</td>
</tr>
<tr>
<td>5.</td>
<td>Mutually agreed key</td>
</tr>
</tbody>
</table>

Fig. 1. EKE-ASK algorithm’s Mutual key agreement phase

3.2 Second Proposal - SPE-ASK

We use SPECKE (Simple Password Elliptic Curve Key Exchange) method introduced in [12]. We calculate $M_U = (sd_U) \times B$ instead of $M_U = d_U \times
B, using pre-shared password ‘s’ and send it to the other side. Also in the other side we use \(M_s = (sd_s) \times B\) instead of \(M_s = d_s \times B\). These changes guarantee its resilience against all possible attacks mentioned above. Figure 2 shows mutual authentication phase, and the main changes to ASK-WAP are shown in bold.

<table>
<thead>
<tr>
<th>User</th>
<th>Server</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. (M_U = (sd_u) \times B)</td>
<td>(M_S = (sd_s) \times B)</td>
</tr>
<tr>
<td>2. Send (M_U)</td>
<td>Receive (M_S)</td>
</tr>
<tr>
<td>3. Generate a random number</td>
<td></td>
</tr>
<tr>
<td>4. Receive (M_S, g_S) (g_S \in {2, n-2})</td>
<td>Send (M_S, g_S)</td>
</tr>
<tr>
<td>5. (M_k = d_u \times M_S) (M_k = d_s \times M_U) (= (sd_u d_s) \times B) (= (sd_s d_u) \times B)</td>
<td></td>
</tr>
<tr>
<td>6. (M_k): Mutually agreed key</td>
<td></td>
</tr>
</tbody>
</table>

*Fig. 2. SPE-ASK algorithm’s Mutual key agreement phase*

### 3.3 Third Proposal - VER-ASK

Another approach to prevent man-in-the-middle attack in ASK-WAP is by encrypting \(M_U\) and \(M_S\) or at least one of them (due to tradeoff between its performance and security goals) using one of ECC encryption/decryption algorithms as in [16][17]. Figure 3 shows the mutual authentication phase, and again the main changes to ASK-WAP are shown in bold.

<table>
<thead>
<tr>
<th>User</th>
<th>Server</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Randomly generate a number (g_u \in {2, n-2})</td>
<td></td>
</tr>
<tr>
<td>2. Send ({g_u B, M_U + g_u M_S}) Receive ({g_U B, M_U + g_u M_S})</td>
<td></td>
</tr>
<tr>
<td>3. (M_U = (M_U + g_u M_S) - d_u \times (g_u B))</td>
<td></td>
</tr>
<tr>
<td>4. Randomly generate a number (g_S \in {2, n-2})</td>
<td></td>
</tr>
<tr>
<td>5. Receive ({g_S B, M_S + g_S M_U}) Send ({g_S B, M_S + g_S M_U})</td>
<td></td>
</tr>
<tr>
<td>6. (M_S = (M_S + g_S M_U) - d_u \times (g_u B))</td>
<td></td>
</tr>
<tr>
<td>7. (M_k = d_u \times M_S) (M_k = d_s \times M_U) (= (d_u d_s) \times B) (= (d_s d_u) \times B)</td>
<td></td>
</tr>
<tr>
<td>8. (M_k): Mutually agreed key</td>
<td></td>
</tr>
</tbody>
</table>

*Fig. 3. VER-ASK mutual authentication phase*

### 3.4 Fourth Proposal - VER-UAP

In regards to UAP weaknesses, if we impose UAP idea to both sides (i.e., user and server) we will be able to remove most of its problems. Figures 4, 5, and 6 illustrate the entire algorithms:

<table>
<thead>
<tr>
<th>User</th>
<th>Server</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Select (d_u \in {2, n-2}) (M_S = d_u \times B)</td>
<td>Receive (M_S)</td>
</tr>
<tr>
<td>2. (M_U = d_u \times B)</td>
<td></td>
</tr>
<tr>
<td>3. Send (M_U)</td>
<td>Receive (M_S)</td>
</tr>
<tr>
<td>4. Compute (d_u^{-1})</td>
<td>Select unique (I_u) and (t_u)</td>
</tr>
<tr>
<td>5. Receive (M_S, I_u, t_u)</td>
<td>Send (M_U, I_s, t_s)</td>
</tr>
<tr>
<td>6. Store (d_u^{-1}, M_U, I_s, t_s)</td>
<td>Store (M_S, i_s)</td>
</tr>
</tbody>
</table>

*Fig. 4. VER-UAP server authentication protocol*

<table>
<thead>
<tr>
<th>User</th>
<th>Server</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Randomly generate a number (g_u \in {2, n-2}) (g_s \in {2, n-2})</td>
<td></td>
</tr>
<tr>
<td>2. (M_M = g_u \times M_S) (M_N = g_s \times M_U) (= (g_u d_u) \times B) (= (g_s d_s) \times B)</td>
<td></td>
</tr>
<tr>
<td>3. Send (M_M)</td>
<td>Receive (M_M)</td>
</tr>
<tr>
<td>4. Receive (M_N)</td>
<td>Send (M_N)</td>
</tr>
<tr>
<td>5. (M_k = d_u^{-1} \times M_N + g_u \times B) (= (d_u^{-1} g_u d_u) \times B) (+ g_u \times B) (= g_u \times B + g_u \times B)</td>
<td></td>
</tr>
<tr>
<td>6. (M_k): Mutually agreed key</td>
<td></td>
</tr>
</tbody>
</table>

*Fig. 5. VER-UAP user authentication protocol*
13. $k_M = H(M_k.x, g_S.g_U)$ \quad k_M = H(M_k.x, g_S.g_U)$

$k_M$ is the unique session key

Fig. 6. VER-UAP authentication and key agreement protocol

In this protocol we don’t need ECDSA in any side; therefore, we have maximum performance in comparison with previous proposed protocols.

4 PERFORMANCE EVALUATION

First we analyze the proposed methods based on various security aspects and compare them according to their performances.

4.1 Security of ASK-WAP Improvements

Due to encryption of transmitted public keys in the first three proposed methods:

i. They provide mutual authentication.

ii. They foil man-in-the-middle attack.

iii. They foil impersonating attack.

iv. They meet known key security and prefect forward secrecy.

Note that the only vulnerability left for SPE-ASK and VER-ASK protocols is ‘known key-share attack’. In this attack an adversary can change their mutual key by multiplying the transmitting public keys with a predetermined integer in order to force them to agree on a desired value. Fortunately, this attack is aborted in the following phases where the ECDSA scheme is used.

4.2 Security of VER-UAP

The security of VER-UAP can be summarized as follows:

i. It provides mutual authentication as same as UAP.

ii. It foils man-in-the-middle and impersonating attacks as same as UAP.

iii. It meets known key security. Compromising $M_k.x$ leads adversary to achieve $(g_U+g_S)$ for and he/she cannot calculate random numbers $g_U$ or $g_S$ separately.

iv. It meets prefect forward secrecy. Compromising private keys $d_U$ and/or $d_S$ doesn’t jeopardize entire system’s security due to choosing independent random numbers $g_U$ and $g_S$

v. Both users and server can initialize communication and there is no difference between them.

vi. $M_k.x$ is used just as the key of symmetric encryption or decryption algorithm.

4.3 Bandwidth, Storage and Computational Load

In order to compare the proposed protocols, we consider three parameters, namely bandwidth, storage requirements and computational load. We use the following values, as mentioned in [11].

$M_L, M_S$: 161 bits
e_U, e_S: 160 bits
$(r_U, s_U), (r_S, s_S)$: 320 bits
t_U, t_S, g_U, g_S: 64 bits

Aydos et al. [9] achieved 1666 bits for transmitting data and 1440 bits for storing data in their protocol.

By calculating the number of transmitting and storing bits in mutual authentication parts of each protocol, we measure the number of storing and transmitting bits in different protocols, as shown in Figure 7 and 8, respectively. For example, by looking at Figure 6 we can see that in stage 3 each party sends a 161 bits point on the elliptic curve (namely $M_k, M_S$). After it in stages 6 and 10 they send encrypted $I$ and $t$ ($I_u, t_u$ for user and $I_s, t_s$ for server) that each of them is 64 bits, thus we send totally $2*64 + 161 = 289$ bits.

In regards to the storage cost, VER-UAP doesn’t need to store $(r, s)$ pair that costs 320 bits. But each party needs to store the public key of another part (i.e., 161 bits). Therefore, there is 320-161=159 bits reduction for storage cost. The total number of storing bits regarding to ASK-WAP is 1440 – 159 = 1281 bits.

Fig. 7. Number of transmitting bits in different protocols
To compare their computational load, we consider the following abbreviations:

- **eP**: Point Multiplication.
- **ECDSA**: Elliptic Curve Digital Signature Algorithm Verification.
- **SKE**: Secret Key Encryption or Decryption.

We have:

- **ASK-WAP**: 
  \[1 \text{ eP}(160 \text{ bits}) + 1 \text{ ECDSA}(160 \text{ bits}) + 2 \text{ SKE} (800 \text{ bits data})\]
- **EKE-ASK**: 
  \[1 \text{ eP}(160 \text{ bits}) + 1 \text{ ECDSA}(160 \text{ bits}) + 4 \text{ SKE} (800 \text{ bits data})\]
- **SPE-ASK**: 
  \[2 \text{ eP}(160 \text{ bits}) + 1 \text{ ECDSA}(160 \text{ bits}) + 2 \text{ SKE} (800 \text{ bits data})\]
- **VER-ASK**: 
  \[4 \text{ eP}(160 \text{ bits}) + 1 \text{ ECDSA}(160 \text{ bits}) + 2 \text{ SKE} (800 \text{ bits data}) + 2 \text{ Point Addition} (161 \text{ bits})\]
- **VER-UAP**: 
  \[3 \text{ eP}(160 \text{ bits}) + 2 \text{ SKE} (128 \text{ bits data}) + 1 \text{ Point Addition} (161 \text{ bits})\]

As can be seen VER-UAP protocol has acceptable performance while meeting security goals as compared to other methods.

**5 CONCLUSION**

We analyzed ASK-WAP and UAP, categorized their advantages and disadvantages. We showed that while UAP is compromising some of ASK-WAP weaknesses, it has some security and communication problems. For example, server cannot initialize the communication, it doesn’t meet perfect forward secrecy, and its block cipher is vulnerable because it uses $M_k,x$ as the main portion of its plain text and its key, simultaneously. By exposing one session key, the server’s private key is discovered. So we proposed three derivations of ASK-WAP, namely, EKE-ASK, SPE-ASK and VER-ASK, and a derivation of UAP called VER-UAP. The EKE-ASK and SPE-ASK are based on pre-shared password, while the VER-ASK is enhancement of ASK-WAP. The VER-UAP adds UAP idea to both sides. The obtained results show the efficiency of our proposed methods while meet the desired security goals. We compared them and showed that VER-UAP has the best performance.

**7 REFERENCES**


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